

The CAPM in an options pricing framework

1. INTRODUCTION

The CAPM of Sharpe (1964), Lintner (1965) and Markowitz (1952) provides a parsimonious framework for understanding the risk-return relationship between securities. It has received (and largely survived) extensive criticism, but despite the theoretical elegance and pedagogic simplicity, it does not satisfy the day to day realities of fund managers. There are possibly several reasons for this, but two in particular are examined in this paper; the definition of risk and the expectations framework of the CAPM.

The CAPM provides an "expectations" framework for security returns. The model estimates expected portfolio (and security) returns on the basis of the risk-free rate, the expected market premium and the expected level of systematic risk i.e. beta. Whilst this is reasonable, the parameters are variables over time, not constants, and the focus on the expected return takes insufficient account of the spread of returns – especially for shorter review periods. Several researchers (e.g. Levy, 1984) have examined the relationship between risk, return and the investment review period. There is considerable debate between practitioners and academics as to whether a longer investment horizon reduces risk (e.g. Butler and Domian (1991) and Bodie, Kane and Marcus (1996)). However, practice suggests that fund managers believe in time diversification, and that they are able to "beat the market" by utilising short term tactics of active portfolio management through asset selection and market timing. Indeed, Jeffery (1984), Sandler (1989) and others have shown that the returns achievable through market timing are dramatically increased (or decreased if accuracy levels are low!) through short review periods. This is particularly true if derivatives are used to effect the switching of assets on account of the considerably reduced transaction costs (Waksman, Sandler, Ward and Firer (1997)). So, whilst the CAPM lends itself to a long term perspective, practice is the opposite.

Furthermore, the CAPM defines risk as "systematic", following Markowitz' (1952) diversification argument. This is perhaps insufficient, as the parameter used to measure systematic risk, beta, does not fully reflect investors' understanding of risk. Specifically, whilst beta excludes non-systematic risk, it makes no distinction between downside risk (loss) and upside potential (profit). Although it is generally accepted that security returns are symmetrical, the

incorporation of option strategies into portfolio management radically changes the shape of the expected return distribution. This paper examines the following proposition: Risk is asymmetric. Investors care about losing, and this is what they mean by "risk". They are not concerned about possible upside potential - just downside loss.

The paper presents some thoughts on using option theory in an attempt to deal with these issues.

2. THE RISK-RETURN PERSPECTIVE

The expected market premium is defined as the expected excess return over the risk-free rate for bearing systematic risk in the market. This is calculated by averaging the excess annual returns generated from the market over the risk-free rate:

$$\text{Expected Market Premium} = 1/n \sum (R_m - R_f) \quad \dots(1)$$

where: R_m = annual return on the market portfolio
 R_f = annual return on the risk free asset
 n = the number of years in the sample

Whilst this may be an acceptable approach in the long-term expected framework of the CAPM, it fails to capture the short-term dynamics of the market. Figure 1 shows a sample of the time-series of the monthly market premium on the JSE.

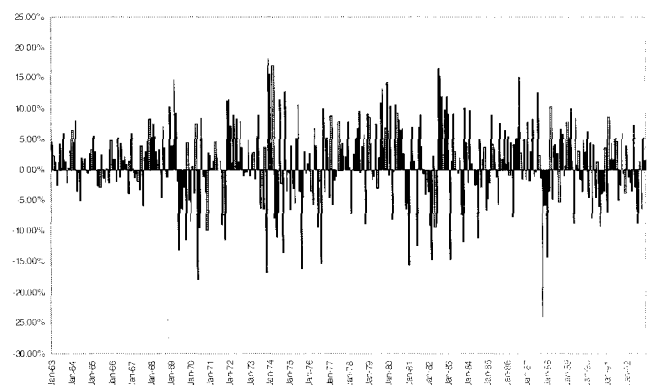


Figure 1: Time-series of the monthly market premium on the JSE

As can be seen from Figure 1, there is considerable short-term variation in the market premium. Active fund managers, confronted with the knowledge that fixed interest securities out-perform equities on occasion, are tempted to engage in market timing

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activities. Certainly, if one accepts that the slope of the Securities Market Line (SML) is not constant but changes dynamically in the short term, one is drawn to the conclusion that investor's indifference curves will intersect tangentially at different points along the SML for short review periods, implying that fund managers *should* engage in market timing. Figure 2 presents the SML from a dynamic perspective:

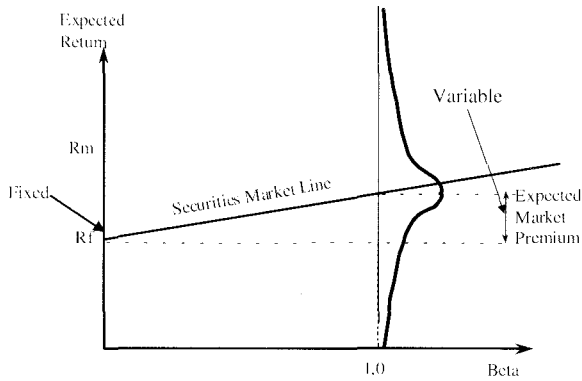


Figure 2: A dynamic representation of the SML

The use of a constant for the market premium in a short-term asset pricing model is therefore oversimplistic. Both the risk-free asset² and the market portfolio follow a distribution of returns and theoretically these are likely to be negatively correlated³.

As can be seen from Figure 2, the slope of the SML follows a distribution for short review periods. In fact, if we assume a fixed risk-free rate, almost 50% of share returns will be below R_f if the portfolio contains any proportion of the Market. This is the simple consequence of a symmetrical distribution of returns. In some instances the SML will slope downwards, and the optimal portfolio is cash, and at other times it will be steeply upward sloping, suggesting a greater portfolio allocation into the market. To the extent then, that fund managers are able to correctly time the market, they should be encouraged to do so.

Most researchers advocate the use of a long term Government bond as a proxy for the risk free rate. Several reasons can be given for this. Firstly, many investment decisions (e.g. company valuations) have a long-term perspective – it therefore makes sense to use a long-term proxy. Secondly, re-investment risk

is avoided with a long-dated asset. Thirdly, the long end of the yield curve is affected primarily by market sentiment – this cannot be said for the short end, which is frequently manipulated by central bankers as an economic lever. However, in South Africa, the so-called “Prescribed Assets” ruling which was in effect in the 1970’s and 1980’s, created an inefficient market in long-term RSA bonds. This has created difficulties in estimating the correct expected market premium and encouraged the use of a short term risk free proxy (see Firer, 1993).

Whilst there are many arguments upholding the use of a long term risk free proxy, a crucial consideration is the investment horizon. It is only possible to achieve a “risk free” return if the investment horizon matches the duration of the risk free asset. If these are miss-aligned, significant re-investment risk is introduced. From a market timing perspective therefore, the use of a short term proxy⁴, appropriately matched to the review period, ensures the risk free rate is in fact a constant – as illustrated in Figure 2.

3. MEASURING RISK

As indicated earlier, the CAPM defines risk in a symmetrical fashion. An investor who introduces a proportion of the market asset into what was previously a pure cash, risk free portfolio, simultaneously introduces systematic risk. The portfolio's expected return is proportionally higher, but subject to a (symmetrical) distribution of possible returns. Contrast this scenario with an investor who uses a portion of the original cash to purchase a call option on the market⁵. Whilst the expected portfolio return can be shown to be higher than the risk free rate and equal (say) to the conventional portfolio, the distribution of returns is not symmetrical and the expected downside risk is limited. Table 1 illustrates the concept.

Table 1 shows four alternative investment scenarios. The first is simply a 100% investment into the risk free asset (R_f) guaranteeing an annualised return of 10%. The second is a conventional portfolio consisting of 50% R_f and 50% the market asset (R_m). The third scenario consists of 97,3% R_f and 2,7%⁶ invested in a one month call option on the market with an exercise price equal to spot. Finally, the fourth scenario consists of a portfolio of 98,1%

² See later discussion on the distribution of the risk free return.
³ Conventional macro-economic policy requires central banks to lower their (short-term) lending rates when the yield curve is high to stimulate the economy and vice-versa to slow down growth when long-term rates are low. Consequently, the expected market premium would be high as short-term interest rates are reduced in anticipation of an expansionary market and vice-versa.

⁴ E.g. a 90 day T-Bill or an interest rate swap.
⁵ Put-call parity ensures that an equivalent scenario would be to hold the Market with a put option on the Market – “Portfolio Insurance” (Hansen (1984)).
⁶ Option prices were calculated using the Black and Scholes option pricing formula for European options. Where options were purchased it was assumed that the cost of the option was deducted from the initial investment capital. Where options were written the premium was added to the initial investment.

the market and 1,9% into a 1 month at-the-money put option.

Table 1: Investment scenarios

Risk free return = 10%		Call Price = 2,7% (B/S)	
Market premium = 6%		Put Price = 1,9% (B/S)	
Market volatility = 20%		Iterations = 1000	
Duration = 1 month			
Exercise price = Spot			

	Investment			
	Rf	Portfolio	Rf+Call	Rm + put
Rf	100,0%	50,0%	97,3%	0,0%
Rm	0,0%	50,0%	0,0%	98,1%
Call	0,0%	0,0%	2,7%	0,0%
Put	0,0%	0,0%	0,0%	1,9%

Mean Return	0,8%	1,1%	1,1%	1,1%
Min	0,8%	-1,0%	-0,2%	-0,2%
Max	0,8%	1,26%	1,86%	1,82%

A Monte Carlo simulation was conducted to compare the risk/return distributions of the four scenarios. The future market level (and hence return) was simulated over 1 000 iterations, using the function⁷ suggested by Winston (1996:143). The results are shown in Table 1 and Figure 3.

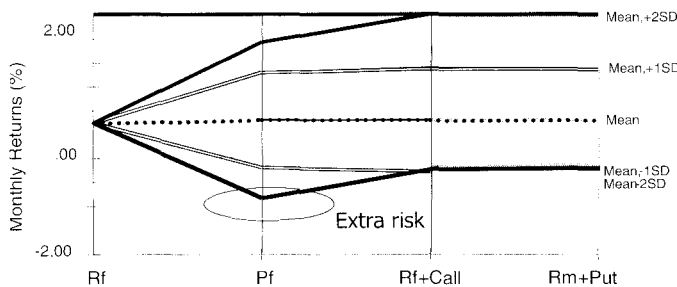


Figure 3: Results from Monte Carlo simulation

Figure 3 and Table 1 show that whilst the expected return is similar for scenarios 2, 3 and 4, the potential minimum return (risk) is greater for scenario 2. Investors might prefer the latter two derivative based portfolios which limit downside risk; but a better definition of downside risk is required before we can come to this conclusion.

The incorporation of derivative products into portfolios suggests that the use of a symmetrical measure of risk such as beta is inappropriate. "Practitioners typically think of risk in terms of the probability and severity of losses, shortfalls or under-performance with respect to a benchmark or goal" (Merrill and Thorley, 1996:13). Following this thought, risk could be more appropriately defined as

⁷ For annual review periods: $P_t = P_0 e^{((Rf - 0.5\sigma^2) + \sigma \cdot N(0,1))}$

This assumes a log-normal distribution of prices.

the probability of under-performing a benchmark, the most obvious being the risk free rate – as illustrated in Figure 4 below:

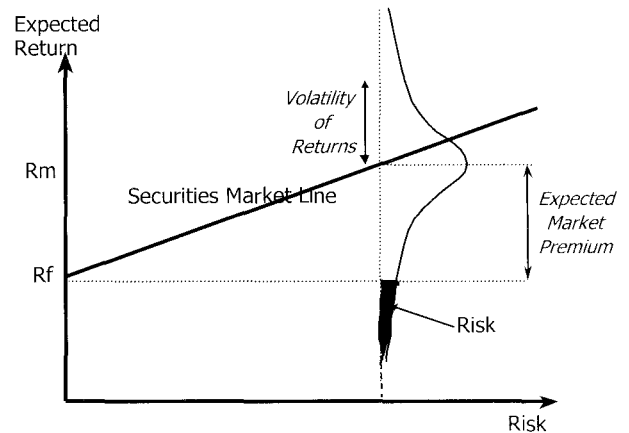


Figure 4: Defining downside risk

Figure 4 illustrates the concept of defining risk in relation to the probability of achieving a return below the risk free rate⁸. Regrettably, it is insufficient to measure risk purely as the probability of attaining returns below Rf, as the shape of the probability distribution will be complex if derivatives are used. The expected value (i.e. "centre of gravity") of the returns below Rf is required. Risk can then be defined as the *expected downside return*. So, for a particular investment strategy there may be a 30% probability that the return will be below Rf. If the average *downside* return is 3%, then the level of risk can be defined as being 7% if Rf is 10% (ie the distance below Rf). The expected downside return is then 30% * 7% = 2,1%. For the purpose of discussion the term *bet*⁹ is used hereafter to refer to the expected downside risk.

From Figure 4 it can be observed that there are two parameters which influence *bet*: the expected market premium and the volatility of returns. Whilst the CAPM incorporates both of these, the latter encapsulated in the beta parameter, *bet* is a more explicit definition of risk as it focuses only on the downside return and can be measured regardless of the shape of the distribution of returns.

Table 2 below shows the relationship between the frequency of returns below Rf, the volatility of returns and the market premium. Table 2 also shows the average value of the downside returns (i.e. the average of the returns below Rf), and hence *bet*, for combinations of volatility and market premium.

⁸ Several other researchers have examined the problem of asymmetric risk, particularly Sortino (1996). The Sortino ratio, a variation of the above, is commonly used to measure downside portfolio risk.

⁹ "*bet*" is simply used for convenience, being the Hebrew equivalent of the Greek beta.

Table 2: Risk, volatility and the market premium

Risk Matrix			
Frequency of returns below the risk free rate			
		Market Premium	
		5%	10%
Volatility	10%	31,0%	15,9%
(Annual SD)	20%	43,1%	33,6%
	30%	48,7%	42,1%

Average value of returns below the risk free rate			
		Market Premium	
		5%	10%
Volatility	10%	3,3%	4,4%
(Annual SD)	20%	-4,5%	-3,1%
	30%	-11,8%	-10,4%

Risk bet			
		Market Premium	
		5%	10%
Volatility	10%	2,1%	0,9%
(Annual SD)	20%	6,3%	4,4%
	30%	10,6%	8,6%

Distance below the risk free rate			
		Market Premium	
		5%	10%
Volatility	10%	6,7%	5,6%
(Annual SD)	20%	14,5%	13,1%
	30%	21,8%	20,4%

Table 2 was calculated by simulating the returns (again using Winston's (1996) formulation to model the distribution of R_m) and measuring the frequency of returns below R_f for different combinations of volatility and different levels of the market premium. The level of risk (*bet*) is then calculated as the expected downside return below R_f , and shown for each combination of volatility and market premium. To illustrate, 48,7% of returns would be below R_f if the annual standard deviation of market returns was 30% and the market premium 5%. The average value of the downside returns (only) would be -11,8% and, for $R_f=10\%$ the distance below R_f would be 21,8%. The expected downside risk (i.e. *bet*) = $48,7\% \times 21,8\% = 10,6\%$.

It is interesting to note that for short review periods, say monthly, whilst the expected return decreases linearly by a factor of 1/12, the standard deviation decreases by a factor of only $1/\sqrt{12}$. There is proportionally greater volatility for shorter review periods, which, from a market timing perspective, is attractive.

For a given market premium and volatility, the level of portfolio risk can be increased by the following strategies:

- Increasingly moving assets from R_f into R_m . This is the conventional approach which, after 100% of the assets are at R_m , requires

borrowing at R_f and re-investing the borrowed funds into R_m .

- Increasingly *writing* options, either by increasing the number of options or by increasing their moneyness. This assumes the investor writes options to earn the premium, but, in doing so, assumes more downside risk.
- Increasingly moving assets from R_f into call options on the market. This can be done by increasing the number of call options or by increasing the moneyness of the call options.
- Variations on the above.

For example, an investor who is long the market may limit downside risk by purchasing put options; "portfolio insurance". The expected portfolio return will decrease because of the cost of the option, but the downside risk distribution has a floor. Alternatively, by writing covered call options, a premium is earned, but the distribution of possible returns is capped and the result more (downside) risky.

We now turn our attention to the risk/return relationship.

Once again, a Monte Carlo simulation was used to compare the risk/return relationship of various portfolios. Variations on four portfolios are shown in Table 3:

Table 3: Portfolio composition

Portfolio	Return
$R_m + R_f$	A conventional portfolio with weightings of R_f and R_m .
$R_f + C$	A call option on the market plus the risk free return for the surplus.
$R_m + P$	A put option on the market plus the market return for the surplus.
$R_m - P$	The market return for the initial capital plus put option premium, less any losses on writing the put.

For each portfolio, three variations of moneyness were examined. Prices for the options were calculated for at-the-money European options and with the strike plus/minus 10% the spot. The risk free rate was fixed

at 10% pa, the market premium at 5%, the volatility of the market at 20% and the term at 1 month. Table 4 presents the results.

Table 4: Monthly risk/return results

		Average Return (Monthly)	Risk Std Devn	Risk Beta	% Under Rf	Expected Downside Risk	Risk Bet
Conventional	Market	1,4%	5,9%	1,00	47,5%	4,3%	2,1%
	Rf25M75	1,2%	4,4%	0,75	47,5%	3,2%	1,5%
	Rf50M50	1,1%	2,9%	0,50	47,5%	2,2%	1,0%
	Rf75M25	0,9%	1,5%	0,25	47,5%	1,1%	0,5%
Calls	RfC+10	0,8%	1,0%	0,09	93,0%	0,2%	0,2%
	RfCATM	1,1%	4,0%	0,62	60,0%	2,3%	1,4%
	RfC-10	1,3%	5,8%	0,99	48,0%	4,3%	2,1%
Puts	RmP-10	1,3%	5,8%	0,99	48,0%	4,3%	2,1%
	RmPATM	1,1%	3,9%	0,60	60,5%	2,2%	1,3%
	RmP+10	0,8%	0,9%	-0,01	57,0%	0,4%	0,2%
Written Puts	Rm-P-10	1,4%	5,9%	1,01	47,0%	4,4%	2,1%
	Rm-ATM	1,6%	8,4%	1,40	38,0%	7,9%	3,0%
	Rm-P+10	1,9%	11,8%	2,01	47,0%	9,0%	4,2%

Table 4 reflects a positive relationship between average return and risk. The average return from the market was 1,4% with $\sigma = 5,9\%$. 47,5% of the portfolio returns were below Rf, the expected downside return was 4,3% below Rf and $bet = 2,1\%$. Rf25M75 represents the conventional portfolio with 25% weighting in Rf and 75% in Rm. The risk/return relationship is linear for risk measured conventionally with beta and when measured with *bet*. Both the at-the-money call strategy (RfCATM) and the at-the-money covered put strategy (RmPATM) show the

same expected return as the Rf50M50 conventional portfolio (1,1%), but all the risk metrics are higher for the option strategies. Unsurprisingly, the in-the-money call strategy (RfC-10) and the out-the-money put strategy (RmP-10) show results which (essentially) mirror the market portfolio. The risk/return results are generally best for the conventional portfolios. Figure 5 shows that the relationship to downside risk is essentially linear for all strategies.

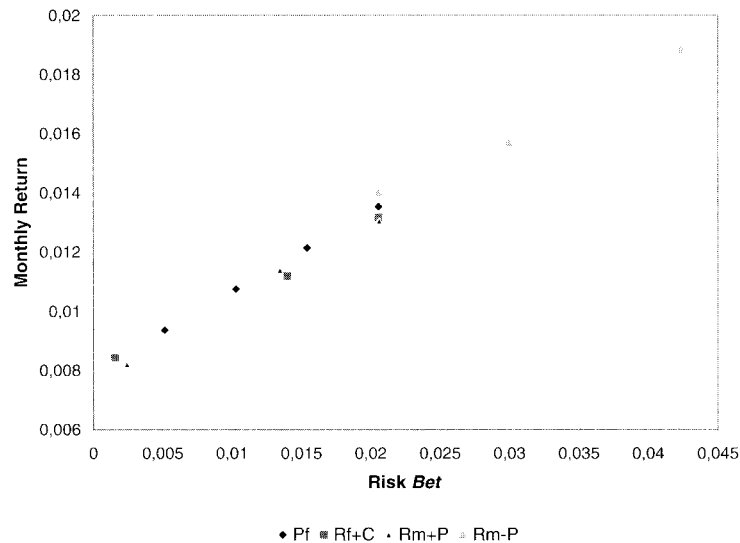


Figure 5: The risk return/relationship for monthly data

Figure 5 shows that the options based strategies produce identical results to conventional portfolios when risk is measured as defined earlier. Higher returns can be attained for greater downside risk, in a linear fashion, by purchasing calls, purchasing puts or writing options.

A further simulation was conducted to explore the relationship between various levels of moneyness for an investor holding R_f and purchasing call options. The resulting risk/return relationship is shown in Table 5 and Figure 6:

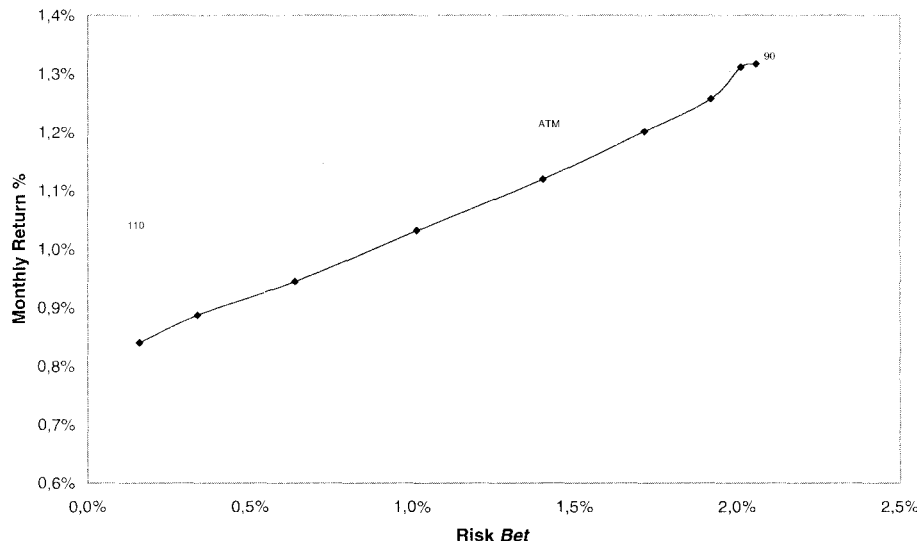


Figure 6: Risk/return graph for a call option portfolio of different strike prices

Table 5: Monthly risk/return data for call options of different strike prices

Strike	90,0	92,5	95,0	97,5	100,0	102,5	105,0	107,5	110,0
Option Cost	10,78%	8,40%	6,21%	4,27%	2,71%	1,57%	0,83%	0,39%	0,17%
Average Return	1,3%	1,3%	1,3%	1,2%	1,1%	1,0%	0,9%	0,9%	0,8%
Std Dev	5,8%	5,6%	5,3%	4,7%	4,0%	3,2%	2,3%	1,6%	1,1%
% Under R_f	47,9%	48,5%	50,6%	54,3%	60,4%	68,8%	78,2%	86,7%	93,0%
Expected Downside	4,3%	4,1%	3,8%	3,2%	2,3%	1,5%	0,8%	0,4%	0,2%
Risk Bet	2,1%	2,0%	1,9%	1,7%	1,4%	1,0%	0,6%	0,3%	0,2%
Risk Beta	1,00	0,96	0,89	0,77	0,61	0,44	0,28	0,16	0,08

Figure 6 shows the linear relationship between downside risk and return for different levels of moneyness. The deeper the call into the money, the greater the expected return. Table 5 gives these figures. One would expect the equivalent result for the strategy of holding the market and purchasing puts of differing strike prices.

The intention of this paper was to examine the expected returns from a short-term market timing

strategy using option based strategies. The call option scenario was further examined. A uniformly distributed random number was used to randomly select "right" and "wrong" decisions for varying levels of timing accuracy. A simulation model was once again used to generate the expected values of various strategies using monthly data, as reflected in Table 6 below.

Table 6: Expected returns for different accuracy levels and different strategies

Accuracy Level	Call Strike Prices					Market Rm	Risk Free Rf	Traditional Timing
	90	95	100	105	110			
100%	3,4%	3,2%	2,5%	1,6%	1,0%	1,2%	0,8%	3,3%
90%	2,9%	2,7%	2,2%	1,4%	1,0%	1,2%	0,8%	2,9%
80%	2,4%	2,3%	1,9%	1,3%	0,9%	1,2%	0,8%	2,4%
70%	1,8%	1,8%	1,6%	1,3%	0,9%	1,2%	0,8%	2,0%
60%	1,6%	1,3%	1,3%	1,0%	0,9%	1,2%	0,8%	1,6%
50%	1,0%	1,0%	1,1%	0,8%	0,8%	1,2%	0,8%	0,9%
40%	0,6%	0,4%	0,7%	0,7%	0,8%	1,2%	0,8%	0,5%
30%	0,2%	0,2%	0,3%	0,6%	0,8%	1,2%	0,8%	0,1%
20%	-0,3%	-0,3%	0,0%	0,4%	0,7%	1,2%	0,8%	-0,6%
10%	-0,7%	-0,6%	-0,3%	0,3%	0,7%	1,2%	0,8%	-0,8%
0%	-1,3%	-1,1%	-0,6%	0,2%	0,6%	1,2%	0,8%	-1,3%

Table 6 shows the expected monthly return for the risk free portfolio was 0,8% and 1,2% for the market. However, for 100% accuracy, a return of 3,4% could be achieved using the deep in-the-money call option strategy, a marginally better result than the traditional

(i.e. switching between Rf and Rm without options) strategy. Figure 7 presents the expected returns and accuracy levels graphically:

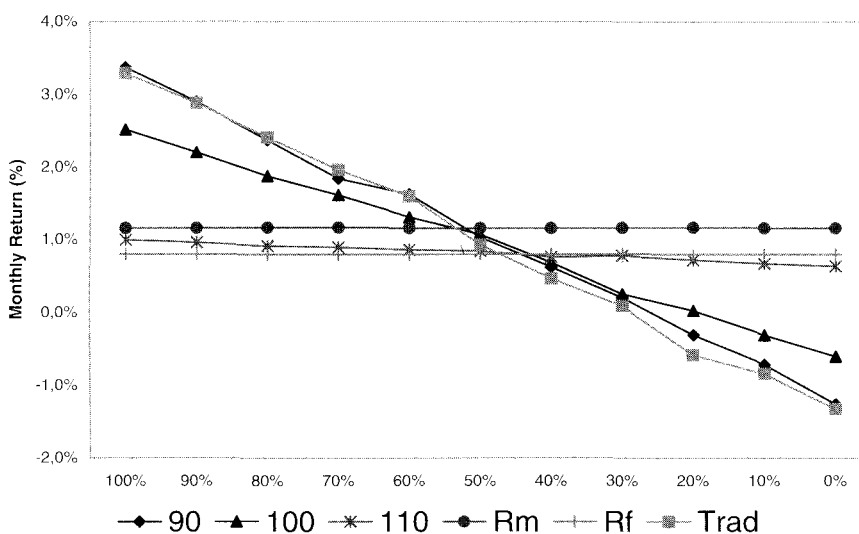


Figure 7: Expected returns for different accuracy levels and different strategies

The deep in-the-money call (90) can be seen to approximate the traditional timing returns for all accuracy levels. The at-the-money call (100) reflects lower upside and lower downside results, and the out-the-money call (110) is almost equivalent to a

buy-and-hold approach. Whilst the relationship between return and timing accuracy is intuitive, the risk return relationship is less so. These results are shown in Table 7 and Figure 8:

Table 7: Risk levels for different market timing strategies

Accuracy Level	Risk Bet					Market Rm	Risk Free Rf	Traditional Timing
	90	95	100	105	110			
100%	0,0%	0,0%	0,0%	0,0%	0,0%	2,1%	0,0%	0,0%
90%	0,2%	0,2%	0,1%	0,1%	0,0%	2,1%	0,0%	0,1%
80%	0,4%	0,4%	0,3%	0,1%	0,0%	2,1%	0,0%	0,4%
70%	0,8%	0,5%	0,4%	0,2%	0,0%	2,1%	0,0%	0,6%
60%	0,8%	0,8%	0,5%	0,3%	0,1%	2,1%	0,0%	0,8%
50%	1,1%	0,9%	0,7%	0,3%	0,1%	2,1%	0,0%	1,1%
40%	1,3%	1,2%	0,8%	0,4%	0,1%	2,1%	0,0%	1,3%
30%	1,4%	1,4%	1,0%	0,5%	0,1%	2,1%	0,0%	1,5%
20%	1,7%	1,6%	1,2%	0,5%	0,1%	2,1%	0,0%	1,7%
10%	1,8%	1,7%	1,3%	0,6%	0,1%	2,1%	0,0%	1,9%
0%	2,1%	1,9%	1,4%	0,6%	0,2%	2,1%	0,0%	2,1%

Figure 8 shows that market timing is worthwhile. The level of downside risk is considerably reduced for all timing strategies. Whilst the expected monthly return is clearly dependent upon the timing accuracy,

even a 50% accuracy level will achieve the same return as a "buy and hold the market" approach, but with only half the downside risk. Waksman *et al* (1997) produced similar results.

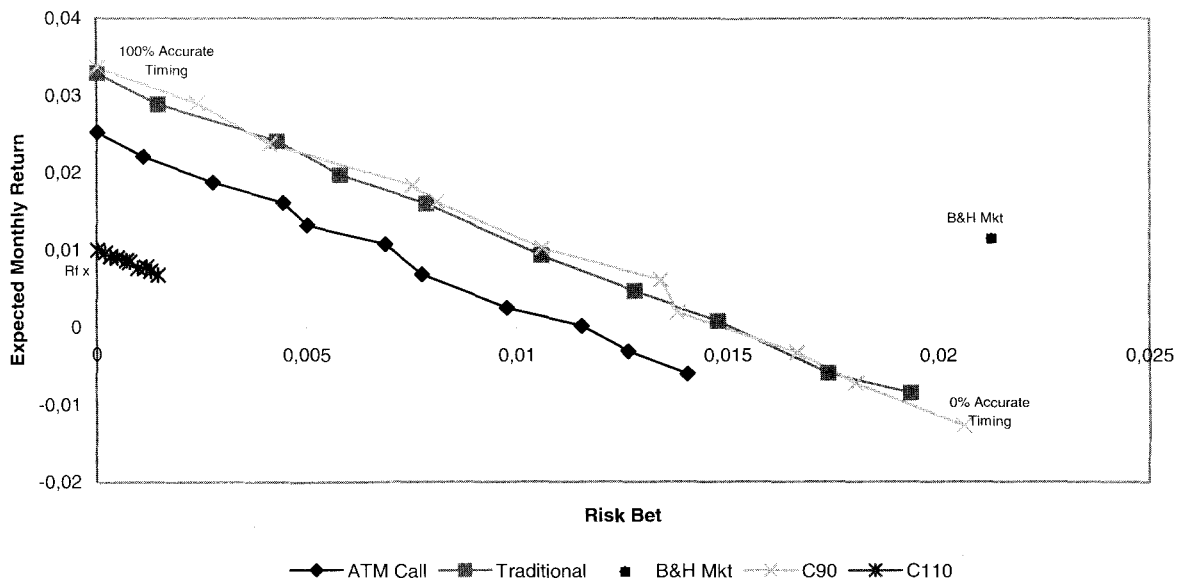


Figure 8: Risk/return relationships for different timing strategies

4. CONCLUSION

This paper combines insights from the CAPM with market timing and option pricing theory for short review periods. The use of an asymmetric approach to measure risk, coupled with the benefits of a dynamic market, are suited to the use of an options pricing framework. The paper suggests the use of an asymmetric measure of systematic risk (*bet*) in place of

beta and illustrates the risk reward payoffs for various positions in an asymmetric risk pricing model. A linear relationship between downside risk (*bet*) and return is found for both conventional strategies and options based approaches. It is shown that the use of options yields equivalent risk related returns. The study confirms the finding of other researchers that, for short review periods, market timing significantly reduces downside risk, and, for reasonable levels of accuracy,

enhances expected returns. An empirical analysis is required to triangulate these findings. Further work is needed to measure downside risk (instead of beta) for individual securities. Additional research is also required to estimate the implied forward market premium from futures prices of options on the market index.

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